Nonlocal gravity

Shuxun Tian Wuhan University

Supervisor: Zong-Hong Zhu Refs: PRD 98, 084040 (2018), PRD 99, 064044 (2019)

2019/04/28@CCNU

- Motivation to modify gravity: The late-time acceleration
- General result to explain the acceleration



Maggiore etal, PRD, 2014

Coincidence problem

The following may be a better theory:

- The late-time acceleration
- Newtonian potential Psi=Phi exactly
- Except kappa=8PiG/c^2, only dimensionless parameters appear in the Lagrangian
- Pure geometric theory

For dimensionless parameters:

- Dimension analysis: [R]=length^{-2}
- If we use R^2, then we need length^2*R^2
- The coefficient length^2 can be a parameter (c/H0 etc), or a math operator (Box^{-1}, an integral operator)
- Box^{-1} → nonlocal gravity

History of nonlocal gravity:

• Deser & Woodard, PRL, 2007 (not Psi=Phi)

$$\Delta \mathcal{L} \equiv \frac{1}{16\pi G} R \sqrt{-g} \times f\left(\frac{1}{\Box} R\right) \,,$$

• Maggiore & Mancarella, PRD, 2014 (not dimensionless)

$$S_{\rm NL} = \frac{1}{16\pi G} \int d^{d+1}x \sqrt{-g} \left[R - \frac{d-1}{4d} m^2 R \frac{1}{\Box^2} R \right],$$

And so on, but none of them satisfy previous 4 requirements

One attempt (Tian, PRD, 2018)

$$\mathcal{L}_G = \frac{1}{2\zeta} \left(R_{\mu\nu} \Box^{-1} R^{\mu\nu} - \frac{1}{2} R \Box^{-1} R \right),$$

- [zeta]=[kappa]
- -1/2 is for Psi=Phi, based on

$$ds^{2} = -c^{2}(1 + 2\Phi/c^{2})dt^{2} + (1 - 2\Psi/c^{2})d\mathbf{r}^{2},$$

 $\Box^{-1} R^{\mu\nu} = 0 \text{ in the background}$

 This assumption has been used in: Koivisto, PRD, 2008; Maggiore & Mancarella, PRD, 2014; Kehagias & Maggiore, JHEP, 2014; Conroy etal, CQG, 2015; etc.

How to set the background?

- Cosmological evolution may give the nonlocal field a nonzero value in the solar system scales.
- Belgacem, Finke, Frassino, and Maggiore, JCAP, 2019 proved this with the McVittie metric.
- And then, Deser2007 and Maggiore2014 (RR model) theories are ruled out by the time-varying G observations. (Belgacem2019)

theory: $|\dot{G}_{\rm eff}/G_{\rm eff}| = \mathcal{O}(H_0)$.

observations: $|\dot{G}/G| < 10^{-12} \text{ yr}^{-1} \approx 0.01 H_0$

Revisit Tian2018 model

$$\begin{split} \mathcal{L}_{G} &= \frac{1}{2\zeta} \left(R_{\mu\nu} \Box^{-1} R^{\mu\nu} - \frac{1}{2} R \Box^{-1} R \right), \\ \mathrm{d}s^{2} &= -c^{2} (1 + 2\Phi/c^{2}) \mathrm{d}t^{2} + (1 - 2\Psi/c^{2}) \mathrm{d}\mathbf{r}^{2}, \\ U_{00} &= f_{10}c^{2} + f_{11}(\mathbf{r})c^{2}, \qquad U_{0i} = 0, \quad U_{\mu\nu} \equiv \Box^{-1} R_{\mu\nu} \\ U_{ij} &= \delta_{ij} f_{20} + \delta_{ij} f_{21}(\mathbf{r}), \end{split}$$

• Results:

Psi=Phi $G_{\text{eff}} = \frac{\zeta c^4}{8\pi [-(f_{10} + f_{20})^2 + f_{10} - f_{20} + 1]},$ $|\dot{G}_{\text{eff}}/G_{\text{eff}}| = \mathcal{O}(H_0).$ Newtonian approximation in nonlocal Gauss-Bonnet gravity

Capozziello etal, PLB, 20

 $\mathcal{L}_G = \frac{1}{2\kappa} (R - \alpha \mathcal{G} \Box^{-1} \mathcal{G}), \quad \text{[alpha]=length^4}$

 $\mathcal{G}=R^2-4R_{\mu\nu}R^{\mu\nu}+R_{\mu\nu\rho\sigma}R^{\mu\nu\rho\sigma},$

$$ds^{2} = -c^{2}(1 + 2\Phi/c^{2})dt^{2} + a^{2}(1 - 2\Psi/c^{2})d\mathbf{r}^{2},$$

 $U = U_0(t) + U_1(\mathbf{r}, t), \qquad U \equiv \Box^{-1} \mathcal{G}$

 $H_0/c \approx \partial/(c\partial t) \ll \partial/(a\partial x)$

$$\gamma \equiv \frac{\Psi}{\Phi} = \frac{c^4/(8\alpha) + 8H^4 + 8H^2\ddot{A} + C_1H/a^3}{c^4/(8\alpha) - 24H^4 + 24H^2\ddot{A} + 16\ddot{A}^2 - 3C_1H/a^3}, \quad \ddot{A} \equiv \ddot{a}/a.$$

$$G_{\text{eff}} = \frac{\kappa c^4}{4\pi (\gamma r_1 + r_2)}, \quad r_1 = \frac{2H^2}{\ddot{A}} + 2 - \frac{48\alpha C_1 H^3}{\ddot{A} a^3 c^4} + \frac{384\alpha H^2 \ddot{A}}{c^4} + \frac{16\alpha C_1 H}{a^3 c^4} - \frac{384\alpha H^6}{\ddot{A} c^4} + \frac{512\alpha H^4}{c^4},$$

$$r_2 = -\frac{2H^2}{\ddot{A}} - \frac{16\alpha C_1 H^3}{\ddot{A}a^3 c^4} - \frac{128\alpha H^6}{\ddot{A}c^4} - \frac{192\alpha H^4}{c^4}.$$

• Generally, $|\dot{G}_{\rm eff}/G_{\rm eff}| = \mathcal{O}(H_0)$. $\Psi \neq \Phi$.

• In the de Sitter phase, Psi=Phi and G_eff is constant.

Summary

- The RT model (Maggiore, PRD, 2014) is the only viable nonlocal gravity theory when confronting observations for now. (Belgacem etal, JCAP, 2019; Tian & Zhu, PRD, 2019)
- Nonlocal gravity may cannot achieve the initial four requirements (Psi=Phi, dimensionless...), and may cannot solve the coincidence problem.

Thanks